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Article

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Article

Design and Potential Power Recovery of Two Types of Energy Harvesting Shock Absorbers

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Abstract: Numerous authors have studied Energy Harvesting Shock Absorbers (EHSA) over the last decade, proposing different designs with diverse geometries, parameters, and components. This article analyzes the energy recovery potential of two types of rotational EHSA, those that use ball-screw and those based on cable transmission. This paper presents the design, manufacturing and mathematical modeling of both options as well as the estimation of the potential power recovery with both technologies. Two types of vehicles are used as references, each one with the characteristic curves of their shock absorbers. Results are presented for different vehicle speeds and road types. Finally, some qualitative characteristics of both EHSAs are detailed to be taken into consideration for their possible use in vehicle suspension.

Keywords: Vibration energy harvesting; suspension; damper; shock absorber; electromagnetic

1. Introduction

The recovery of energy from different areas of the vehicle is a topic that has attracted the attention of many researchers in recent years, resulting in a large number of publications. A considerable number of references propose harvesting energy from: the heat given off by the exhaust pipes [\[1](#page-18-0)[–5\]](#page-18-1), the absorption of the kinetic energy in the brakes [\[6–](#page-19-0)[9\]](#page-19-1), the deformation of the tires [\[10,](#page-19-2)[11\]](#page-19-3), the vibrations of the engine [\[12](#page-19-4)[,13\]](#page-19-5), the seats [\[14\]](#page-19-6), and also the suspension system of the vehicle [\[15\]](#page-19-7).

The energy recovery in the suspension system, more specifically in the shock absorber, is carried out with Energy Harvesting Shock Absorbers (EHSA). Abdelkareem et al. [\[16\]](#page-19-8) and Zhang et al. [\[17\]](#page-19-9) made a review of all the EHSA technology that have been presented up to the present time. These systems usually work generating a magnetic field variation around a winding, resulting in a current and an electrical voltage. This variation of magnetic field can be generated in two ways—linearly and/or rotationally. Tang et al. [\[18\]](#page-19-10) and Singh et al. [\[19\]](#page-19-11) have proposed linear electromagnetic dampers. In the first reference, the authors obtain a power of 26–33 W at an excitation speed (piston velocity of the damper) of 0.25 m/s, while for the second the power is 160 W at a speed of 0.1 m/s. On the other hand, Zhang et al. [\[20\]](#page-19-12) presented a system in which they duplicate the relative speed between the magnetic field and the conductor, multipliying the generated power by four.

There are several types of rotational electromagnetic dampers. As the movement in the vehicle suspensions is translational, the generation of a rotationally variable magnetic field requires a mechanism that converts translation into a rotation. These are well-known systems: rack-pinion [\[21](#page-19-13)[–23\]](#page-19-14), hydraulic [\[24–](#page-19-15)[29\]](#page-19-16), ball-screw [\[30](#page-20-0)[–33\]](#page-20-1), and some more exotic such as the "Linkage mechanism" [\[34\]](#page-20-2), "Two-Leg motion" [\[35\]](#page-20-3), or using flywheel drive [\[36\]](#page-20-4). All these systems have their own equivalent inertias, backlashes, and frictions affecting the dynamic behavior of the shock absorber and, therefore, the vehicle.

One of the main difficulties when analyzing the EHSAs found in the literature is the lack of a common strategy to compare the different systems. Most authors present original designs but focus their attention on achieving different objectives: generate the maximum amount of power, have a certain damping coefficient, have a damping force or obtain the maximum efficiency in the system, etc.

In this article, two types of rotational EHSA are compared under a common framework. The EHSAs that use the ball-screw transmission system, known as the Ball-Screw Energy Harvesting Shock Absorber (BS-EHSA), and the EHSAs that use the cable transmission system, also known as the Cable-Dynamic Energy Harvesting Shock Absorber (CD-EHSA). The main objective of this work is to compare quantitatively and qualitatively an innovative EHSA design (CD-EHSA) with one found in the literature (BS-EHSA). In addition, to provide reliable data of the potential that both systems have in the recovery of energy from the suspension of vehicles.

The main contributions of this work concentrate on four aspects:

- 1. The design, manufacture, and mathematical modeling of the systems: BS-EHSA and CD-EHSA.
- 2. The results, experimental and simulation of the electrical power that is generated with both technologies for different conditions. Taking as reference the characteristic curves of the damper of a Renault Twizy and Ford Focus.
- 3. The results shown in this work, both for the BS-EHSA and for the CD-EHSA, make it possible to compare each other because they share the same initial conditions.
- 4. Qualitative analysis of both technologies for their future application in vehicle suspension systems.

This article is divided into seven sections. The first being the introduction, the second section describes under which common framework the prototypes have been manufactured. The third section shows the design, the prototype, and mathematical model of the BS-EHSA, while the fourth section does the same for the CD-EHSA. The fifth section details the conditions that have been established to evaluate the potential of both the BS-EHSA and CD-EHSA in energy recovery in the vehicle's damping. In the sixth section the results are presented, together with a qualitative analysis of the characteristics of both systems. In the last section, some conclusions of the work are presented.

2. Framework to Analyze the Performance of the BS-EHSA and CD-EHSA

The rotational EHSAs contain a characteristic design parameter: feed rate per revolution (FRR), normally given in mm/rev. This parameter varies in the literature [\[21](#page-19-13)[,33,](#page-20-1)[37\]](#page-20-5) between 4–6 mm/rev. In the prototypes presented below, it has been decided to choose the value of 5 mm/rev. Therefore, both systems, the BS-EHSA and CD-EHSA, are designed with the same feed value.

The same generator is installed in both prototypes (Maxon 218010), which is also the one used by Li et al. [\[37\]](#page-20-5). Table [1](#page-3-0) shows the specifications of this generator.

Rated Voltage	Rated Speed	Max Permissible Speed	Rated/Max Current	Internal Resistor R_i	Internal Inductance L	Torque Constant K_t	Voltage Constant $1/K_{re}$
48 V	2700 r/min	12,000 rpm	1.38 A	6.6Ω	1.7 mH	0.137 nm/A	69.7 rpm/V

Table 1. Parameters of the Maxon Motor 218,010 used in the prototype.

This way with the same generator and the same translation into a rotation parameter, the difference that will exist between the BS-EHSA and the CD-EHSA will only be the translation into a rotation transmission system, which implies differences in equivalent inertia, backlash, and internal friction. This applies to Sections [3](#page-4-0) and [4,](#page-7-0) where both EHSAs share the same design parameters. However, in Sections [5](#page-11-0) and [6,](#page-16-0) the design parameters are changed at this time with the intention to match the characteristic curves of the dampers of a Renault Twizy and a Ford Focus.

For the mathematical modeling of both systems, the equivalent mechanical model presented in Figure [1](#page-4-1) will be used. This consists of deriving from the equations of the dynamics of each system a coefficient of: equivalent mass *meq*, also known as inerter [\[38\]](#page-20-6), an equivalent damping coefficient *ceq*, and an equivalent stiffness coefficient *keq*, as proposed by Bowen et al. [\[15\]](#page-19-7), as in Equation (1).

$$
F = m_{eq}\ddot{x} + c_{eq}\dot{x} + k_{eq}x \tag{1}
$$

Figure 1. Equivalent mechanical system configuration for the Energy Harvesting Shock Absorbers
 TUCA (EHSA).

3. Ball-Screw Energy Harvesting Shock Absorber (BS-EHSA)

3.1. Design Principle and Prototype

The Ball-Screw Energy Harvesting Shock Absorbers (BS-EHSA) as the name implies, uses a ball-screw transmission system to go from translation into rotation. Figure [2](#page-4-2) shows an example of this type of shock absorber, which is composed of a nut, a screw, and a coupled generator. Table [2](#page-4-3) specifies the design parameters of this type of damper.

Figure 2. Left: Photo of the (Ball Screw) BS-EHSA prototype. Right: CAD model of the BS-EHSA.

Table 2. Main characteristics of the Ball-Screw Energy Harvesting Shock Absorber.

Parameters		Value	Units
Inertia of motor	I m	121	gcm^2
Inertia of screw	Is	180	gcm ²
Ball center-to-center diameter	d_s	16	mm
Screw lead	Τ	h	mm/rev

3.2. Mathematical Model

For the derivation of the equivalent mechanical model, the equations of the dynamics of the system of Figure [3](#page-5-0) are used: .

$$
\eta_{bs} F_a \dot{x} = J_s \dot{\theta}_s \ddot{\theta}_s + \tau_g \dot{\theta}_g \tag{2}
$$

Equation (2) represents the ball-screw energy balance of the generator, where η_{bs} is the ball screw efficiency, *F^a* is the damping force, x is the linear displacement, τ*^g* is the torque over the screw, and θ_s *and* θ_g represent the rotation of the screw and the generator:

$$
\tau_g = J_m \ddot{\theta}_g + c_m \dot{\theta}_g + k_m \theta_g \tag{3}
$$

Equation (3) represents the dynamic behavior of the generator, where *Jm* is the rotational inertia, c_m is the rotational damping, and k_m represents the rotational stiffness of the generator:

$$
\theta_s = \theta_g; \quad x = \frac{\theta_s \tau}{2\pi} \tag{4}
$$

Equation (4) accounts for the relationships among rotational and linear displacements.

Figure 3. The dynamic model of the Ball-Screw Energy Harvesting Shock Absorber.

These equations were previously derived by Li et al. [\[37\]](#page-20-5). Operating with the equations, their equivalent mechanical model coefficients (1) are:

$$
m_{eq} = (2\pi)^2 \frac{J_m + J_s}{\eta_{bs} \tau^2}
$$
\n(5)

$$
c_{eq} = (2\pi)^2 \frac{K_t K_{re} (R_e + R_i)}{\tau^2 \eta_{bs} ((R_e + R_i)^2 + L_i^2 \omega^2)}
$$
(6)

$$
k_{eq} = (2\pi)^2 \frac{K_t K_{re} L_i \omega^2}{\tau^2 \eta_{bs} ((R_e + R_i)^2 + L_i^2 \omega^2)}
$$
(7)

3.3. Comparison of Simulations and Experiments

To simulate the dynamics of the BS-EHSA, the Simscape/Mathworks® program and the above are used. Armstrong et al. [\[39\]](#page-20-7) introduced a friction model for all the moving parts and it was used here.

Figure [4](#page-6-0) shows some of the simulations and experimental results, which show that the computational model is able to reproduce the force and the voltage results obtained in the experimental setup.

Figure 4. Comparison of experimental and simulation results for the BS-EHSA. Top: Damping force. Bottom: Voltage at the generator.

were run between 0.5–3 Hz using different load electrical resistances (15, 47, 62, 94, and 109 Ω). Figure [5](#page-6-1) shows the test bench used for the BS-EHSA prototype (an MTS 835 machine). The tests The acquisition system is composed of a CompactRio NI cDaq-9178 module and a NI-9234 module. The results of the experimental tests can be seen in Figure [6.](#page-7-1) The graphs show that, as indicated by the equations, when the excitation frequency increases or when the external load decreases, the energy recovered by the BS-EHSA increases. Additionally, it can be seen that the damping coefficient will depend on the resistance that is connected to the generator.

Figure 5. Bench test setup for the BS-EHSA.

Figure 6. Top-Left: Force-displacement loop at different electrical loads. Top-Right: Force-displacement loop at different excitation frequencies. Bottom: Force-velocity graph at 1.0 Hz and 10 mm amplitude for 15 and 47 ohms.

4. Cable-Dynamics Energy Harvesting Shock Absorber (CD-EHSA)

4.1. Design Principle and Prototype

The Cable-Dynamic Energy Harvesting Shock Absorbers (CD-EHSAs) use a steel cable and a pair of pulleys as the main element for the translational into rotational conversion. Figure [7](#page-7-2) shows an example of such a shock absorber. The translation movement of the suspension is transferred through a piston (1) to a sliding part running on linear guides (2). The sliding part has two preloaded cables (3) that displace it. The cable is connected in one end to a driven pulley (4) and to the other end to a generator pulley (5), which is connected to another larger pulley (6). This one is connected through a band to a smaller pulley (7) that doubles the rotational speed. The smaller pulley is rigidly assembled to a multiplier (8) connected to an electric generator (9). Table [3](#page-8-0) specifies the design parameters of this type of shock absorber.

Figure 7. Left: Photo of the (Cable Dynamics) CD-EHSA prototype. Right: Cad model of the CD-EHSA.

Parameters		Value	Units
Inertia of motor	I_m	121	gcm ²
Inertia of the multiplier	$\mathsf{Im}u$	100	gcm ²
Inertia of the 1st pulley	J_{pt1}	233	gcm ²
Inertia of the 2nd pulley	J_{pt2}	81	gcm ²
Multiplier ratio	k_{mu}	5	
Generator pulley radius	R_{pg}	8	mm
Cable stiffness coefficient	k_c	1104	kN/m
Cable damping coefficient	c_c	100	N/(m/s)

Table 3. Main characteristics of the Cable-Dynamic Energy Harvesting Shock Absorber.

4.2. Mathematical Model

For the derivation of the equivalent mechanical model, the equations of the system dynamics of Figure [8](#page-9-0) are used as follows:

Relationship between input force and tensors:

$$
F_a = T_2 - T_1 \tag{8}
$$

Balance of energy in generator pulley:

$$
\eta_{pg}(T_1 - T_3)R_{pg}\dot{\theta}_{pg} = J_{pg}\ddot{\theta}_{pg}\dot{\theta}_{pg} + \tau_{pg}\dot{\theta}_{pg}
$$
\n(9)

Balance of forces in each of the two tensors:

$$
T_1 = k_c(x_1 - x) + c_c(\dot{x}_1 - \dot{x})
$$
\n(10)

$$
T_2 = k_c(x - x_2) + c_c(\dot{x} - \dot{x}_2)
$$
\n(11)

Preload in the cable:

$$
T_3 = k_p(x_2 - x_1) + T_p \tag{12}
$$

Balance of moments in the driven pulley:

$$
(T_2 - T_1)R_{pl} - J_{pl}\ddot{\theta}_{pl} = 0
$$
\n(13)

Relationships between the angular velocity of the pulleys and the displacements:

$$
\dot{\theta}_{pl} = \frac{\dot{x}_2}{R_{pl}} \tag{14}
$$

$$
\dot{\theta}_{pg} = \frac{\dot{x}_1}{R_{pg}} \tag{15}
$$

Balance of energy in transmission pulley 1 and 2:

$$
\eta_{pt1}(\tau_{pg}\dot{\theta}_{pg}) = J_{pt1}\ddot{\theta}_{pg}\dot{\theta}_{pg} + (T_{t2} - T_{t1})R_{pt1}\dot{\theta}_{pg}
$$
\n(16)

$$
\eta_{pt2}(T_{t2} - T_{t1})R_{pt2}\dot{\theta}_{pt2} = J_{pt2}\ddot{\theta}_{pt2}\dot{\theta}_{pt2} + \tau_{pt2}\dot{\theta}_{pt2}
$$
\n(17)

Balance of energy in the multiplier:

$$
\eta_{mu}(\tau_{pt2}\dot{\theta}_{pt2}) = J_{mu}(\ddot{\theta}_{mu} - \ddot{\theta}_{pt2})(\dot{\theta}_{mu} - \dot{\theta}_{pt2}) + \tau_{g}\dot{\theta}_{mu}
$$
\n(18)

Relationships between the angular displacements, velocities, and radiuses of the pulleys:

$$
\theta_{mu} = \theta_g \tag{19}
$$

$$
\frac{R_{pt1}}{R_{pt2}} = \frac{\dot{\theta}_{pt2}}{\dot{\theta}_{pt1}}
$$
\n(20)

$$
k_{mu} = \frac{\dot{\theta}_{mu}}{\dot{\theta}_{pt2}}
$$
 (21)

$$
k_{pt} = \frac{R_{pt1}}{R_{pt2}}\tag{22}
$$

Dynamic behavior of the generator:

$$
\tau_g = J_m \ddot{\theta}_g + c_m \dot{\theta}_g + k_m \theta_g \tag{23}
$$

Figure 8. The dynamic model of the Cable-Dynamic Energy Harvesting Shock Absorber.

– Equations (8)–(15) refer to the transmission of the movement from the cable to the pulleys, and the rest relate to the dynamic behavior of the transmission pulleys, the multiplier, and the generator. Operating with the equations, the equivalent mechanical model coefficients (1) are obtained:

$$
m_{eq}^{*} = \frac{1}{R_{pg}^{2} \eta_{pt1} \eta_{pg}} \left(J_{pt1} + J_{pg} + \frac{k_{pt}^{2}}{\eta_{pt2}} \left(J_{pt2} + J_{mu} - 2J_{mu} k_{mu} + \frac{k_{mu}^{2} (J_{mu} + J_{m})}{\eta_{mu}} \right) \right)
$$
(24)

$$
c_{eq}^{*} = \frac{k_{mu}^{2}k_{pt}^{2}K_{re}K_{t}(R_{e} + R_{i})}{R_{pg}^{2}\eta_{pt1}\eta_{pg}\eta_{pt2}\eta_{mu}((R_{e} + R_{i})^{2} + L_{i}^{2}\omega^{2})}
$$
(25)

$$
k_{eq}^{*} = \frac{k_{mu}^{2} k_{pt}^{2} K_{re} K_{t} L_{i} \omega^{2}}{R_{pg}^{2} \eta_{pt1} \eta_{pg} \eta_{pt2} \eta_{mu} ((R_{e} + R_{i})^{2} + L_{i}^{2} \omega^{2})}
$$
(26)

$$
m_{eq} = \frac{\left(m_{eq}^{*}c_{c}^{2} - m_{eq}^{*}2k_{c}\right)\omega^{2} + 2m_{eq}^{*}k_{eq}^{*}k_{c} + m_{eq}^{*}k_{c}^{2} - c_{eq}^{*}2k_{c} - k_{eq}^{*}c_{c}^{2}}{\left(k_{eq}^{*} + k_{c} - m_{eq}^{*}\omega^{2}\right)^{2} + \left(c_{eq}^{*} + c_{c}\right)^{2}\omega^{2}}
$$
(27)

$$
c_{eq} = \frac{\left(c_{eq}^{*}{}^{2}c_{c} + c_{eq}^{*}c_{c}^{2} - 2k_{eq}^{*}c_{c}m_{eq}^{*}\right)\omega^{2} + m_{eq}^{*}{}^{2}c_{c}\omega^{4} + c_{eq}^{*}k_{c}^{2} + c_{ck}^{*}k_{eq}^{2}}{\left(k_{eq}^{*} + k_{c} - m_{eq}^{*}\omega^{2}\right)^{2} + \left(c_{eq}^{*} + c_{c}\right)^{2}\omega^{2}}
$$
\n(28)

$$
k_{eq} = \frac{k_{eq}^{*} k_c + k_{eq}^{*} k_c^{2}}{\left(k_{eq}^{*} + k_c - m_{eq}^{*} \omega^{2}\right)^{2} + \left(c_{eq}^{*} + c_c\right)^{2} \omega^{2}}
$$
(29)

4.3. Comparison of Simulations and Experiments

The Simscape/Mathworks® program is also used to simulate the dynamics of the CD-EHSA using the above equations and the same friction model that is in the BS-EHSA case. Experimental results fitting computational ones are shown in Figure [9.](#page-10-0)

Figure 9. Comparison of experimental and simulation results for CD-EHSA. Top: Damping force. Bottom: Voltage at the generator.

Experimental tests were also run in the MTS 835 machine (Figure [10\)](#page-11-1). The results are presented in Figure [10.](#page-11-1) The same excitation frequencies and loads as in the BS-ESHA case were used. The tests were carried out for the same excitation frequencies and resistance load as in the case of the BS-EHSA. Obtained for each were the damping force values and the generator voltage. Figure [11](#page-11-2) shows, as for the BS-EHSA, that the behavior of the CD-EHSA is affected by changing both the excitation frequency and the external load that is connected to the generator.

Figure 10. CD-EHSA bench setup.

Figure 11. Top-Left: Force-displacement loop at different electrical loads. Top-Right: Force-displacement loop at different excitation frequencies. Bottom: Force-velocity graph at 0.5 Hz and 10 mm amplitude for 15 and 47 ohms.

5. Numerical Simulation using BS-EHSA and CD-EHSA

In Sections [3](#page-4-0) and [4,](#page-7-0) both EHSAs share the same feed rate per revolution (FRR) parameter and generator. However, in the simulation presented in this section and in Section [6,](#page-16-0) both parameters are changed (FRR and generator) in order to match the characteristic curves of the dampers of a Renault Twizy and a Ford Focus.

5.1. Vehicle Parameters and Modelling

This section details the boundary conditions that have been established to analyze the potential of both the BS-ESHA and the CD-EHSA for energy recovery in the vehicle suspension. For this, a model of a complete car with 7 degrees of freedom has been implemented, as shown in Figure [12](#page-12-0) (right), the equations of both EHSAs are used to represent the dampers. The data are taken from two types of vehicles: a single-seater (Renault Twizy 45) and a 5-passenger car (Ford Focus), the table in Figure [12](#page-12-0) (left) summarizes the main parameters.

Figure 12. Left: Geometric, mass, and inertia properties of both vehicles (Renault Twizy and Ford Focus). Right: Full vehicle model of a 7 DOF having EHSAs instead of the damper systems.

5.2. Input Signals Generation

As an input signal for this model $\left(x_{0}\right)$, standardized road profiles according to ISO 8608 are used. For the two front wheels, a unit noise power signal (using the Simulink® program) is generated passing through a low-pass filter:

$$
G(s) = \frac{2\pi n_0 \sqrt{G_q u}}{s + 2\pi f_0}
$$
\n(30)

where $G_q(n_0)$ is the roughness coefficient of the road in m^3 ; n_0 is a reference for the spatial frequency that is equal to 0.1. m^{-1} ; *f*₀ is the initial cut-off frequency that has a value of 0.0628 Hz and *u* is the ⁄ speed of the vehicle in *m*/*s*. These data were obtained from the work of Abdelkareem et al. [\[40\]](#page-20-8).

For the generation of the signal of the rear wheels, the method proposed by Ren et al. [\[41\]](#page-20-9) is used. It allows a delay of the signal of the front wheels depending on the speed and length of the vehicle. This method consists of multiplying the signal of the front wheels by the transfer function:

$$
H_{FR} = \frac{\frac{\tau_s^2}{12}s^2 - \frac{\tau_s}{2}s + 1}{\frac{\tau_s^2}{12}s^2 + \frac{\tau_s}{2}s + 1}
$$
(31)

where $\tau_s = \frac{(a+b)}{u}$, $(a+b)$ is the distant $\frac{f^{(n)}(u)}{u}$, $(a + b)$ is the distance between the front and rear wheel. In Figure [13](#page-13-0) you can see the logarithmic graph of the PSD of the three types of road, both for the right and left wheels. The graphs show that the signals generated as input to the complete car system have the same theoretical slope as stipulated by ISO 8608. In the same figure, an example of a road profile is shown, driving at 100 km/h in a class C profile (Table [4\)](#page-13-1).

Figure 13. Roll mode input at a vehicle driving speed of 100 km/h. Top: Logarithmic PSD of the road profiles for the right and left wheels. Bottom: Vehicle front and rear wheel inputs.

Road Level	$G_q(n_0)(x10^{-6})m^3$ $n_0 = 0.1 m^{-1}$			
	Lower Limit	Average	Upper Limit	
А	8	16	32	
B	32	62	128	
	128	256	512	
	512	1024	2048	
E	2048	4096	8492	
F	8192	16,384	32,768	

Table 4. Classification standard of 6 road roughness levels.

5.3. EHSA Design

the Renault Twizy it is ±0.1 m/s. Figure [15](#page-14-1) shows the average speeds we will have between the ends of the suspension driving on road types A and B (Table [4\)](#page-13-1). Their values are within the range established For the design of both EHSA, the force-speed curves of the dampers of a Renault Twizy and a Ford Focus are used, as can be seen in Figure [14.](#page-14-0) Both EHSAs have been designed so that they have the same damping value at low speeds. In the case of the Ford-Focus, it is ± 0.15 m/s and in the case of as low speeds.

In order to obtain a different damping in compression and extension movements in the EHSA, the diode system proposed by Zhongjie et al. [\[37\]](#page-20-5) is used, in this way different values of electrical resistance can be used depending on the direction of rotation of the generator.

The three most important parameters in the design of the rotational EHSA are: the feed rate per revolution (FRR) (mm/rev), the electromagnetic constant of the generator (rpm/V), and the electrical resistance connected to the generator $(Ω)$. Both EHSAs require the same damping characteristics as the dampers already installed in both vehicles, therefore the design parameters presented in Table [5](#page-15-0) have been chosen. The tables illustrate that for the Renault Twizy the Maxon 218,010 (Table [1\)](#page-3-0) is used and for the Ford Focus, the Maxon 136,210 is used (Table [6\)](#page-15-1). The limitations of the generators are in their maximum allowed speed and in their maximum current. From Figure [15,](#page-14-1) it can be seen that none of the generators, either using the BS-EHSA and/or the CD-EHSA in the four dampers, exceeds the permitted speed limit (12,000 rpm). The same applies to the induced current (Figure [16\)](#page-16-1). The average current circulating inside the generator is kept below its maximum values all the time.

Figure 14. Force-velocity curve from the CD-EHSA, BS-EHSA, and the vehicle's damper. Top: Ford Focus. Bottom: Renault Twizy.

Figure 15. Generator speed from the CD-EHSA and BS-EHSA and the relative velocity in the four suspension system of the Renault Twizy and Ford Focus.

Table 6. Parameters of the Maxon Motor 136,210 used in the simulation.

Rated Voltage	Rated Speed	Max Permissible Speed	Rated/Max Current	Internal Resistor R_i	Internal unductance.	Toraue Constant <i>k+</i>	Voltage Constant $1/k_{re}$
24 V	7970 r/min	'2,000 r/min		0.143Ω	0.056 mF	0.0263 nm/A	364 rpm/V

Figure 16. Generator current from the CD-EHSA and BS-EHSA in the four suspension system of the Renault Twizy and the Ford Focus. The red line indicates the maximum current of the generator.

6. Results and Discussion

With the conditions described in the previous section, Figures [17](#page-16-2) and [18](#page-17-0) show an estimation of the average power that can be generated with both EHSAs in the Renault Twizy and/or the Ford Focus. From the graphs, it can be seen that the power level increases with the speed of the vehicle and the roughness of the pavement. n and to show an exempt in the previous section, rights in and to show an estimation

Figure 17. Mean power generated from the BS-EHSA and CD-EHSA on a Renault Twizy at different driving speeds and road roughness. The results take into account the four EHSAs.

Using the same approach as Múčka et al. [\[42\]](#page-20-10), it can be deduced that the power that would be generated circulating at 120 km/h with the Ford Focus in the case of German roads ($\tilde{G}_q(n_0)=100\cdot10^{-6}$ m³) would be between 350–500 W, for Chinese roads ($G_q(n_0) = 270 \cdot 10^{-6} \text{m}^3$) it would increase to 400–700 W,

and for roads in Eastern Europe ($G_q(n_0) = 400\cdot 10^{-6}$ m³) it would be between 700–1200 W. Keep in mind that in all these results, the vehicle is driving in a straight line at a constant speed. Neither the curves, nor the cant on the roads, nor the accelerations or decelerations of the vehicle are taken into account, all these conditions would only increase the power generated by the EHSA.

Figure 18. Mean power generated from the BS-EHSA and CD-EHSA on a Ford Focus at different driving speeds and road roughness. The results take into account the four EHSAs.

With respect to the difference in power generation, 80–110% more can be generated using the CD-EHSA system compared to the BS-EHSA. One of the main causes explaining why the CD-EHSA system allows a greater power generation compared to the BS-EHSA is that internal inertia is much lower. The electrical power obtained from a generator is proportional to the square of the current flowing through its coils. If we look at Figure [16,](#page-16-1) we can see that the average current flowing through the CD-EHSA is higher than the BS-EHSA. This is because there is a greater force for the electromagnetic torque of the generator when the inertial force is lower.

Below (Table [7\)](#page-17-1) are some advantages and disadvantages in the use of the CD-EHSA or the BS-EHSA as a damping system in the vehicle.

7. Conclusions

This article addresses two types of rotational EHSA. The EHSAs that use the ball-screw transmission (BS-EHSA) and the EHSAs that use the cable transmission (CD-EHSA). For both systems, their mathematical model has been presented as well as a prototype with their respective experimental tests.

Once the simulation results are compared with the experimental tests, simulations were carried out to obtain the energy recovery potential that both technologies generate under different boundary conditions. The characteristic curves of the shock absorbers of a Renault Twizy and a Ford Focus were used. As an example, an estimate of power generation between 500–1000 W is obtained on an old pavement road (class C road) with a 5-passenger car at a speed of 120 km/h. The results also show that the CD-EHSA system can generate between 80–110% more power than with the BS-EHSA.

The EHSAs are technologies whose final aim is replacing conventional shock absorbers that are at present used on most, if not all, vehicles. For this reason, they must be able to provide the same dynamic behavior than conventional shock absorbers, but also have the same durability and provide the same comfort to the passengers. This paper gives some qualitative data on the BS-EHSA and CD-EHSA technologies that can be used in the development of energy recovery technologies in the suspension. Much has to be done still on the durability aspects that are directly related to the design and the selection of components, which has a direct implication on cost.

The results shown in this article are only theoretical. However, the frictions that may exist in the BS-EHSA and the CD-EHSA have been taken into account in the computational models. In addition, the power estimations summarized in this paper consider that the vehicle is traveling on a straight road at different speeds and road surface quality, and not taking into account other events in the vehicle suspension that exist that can increase the amount of harvested energy, such as the passage through curves, accelerations, and braking, etc.

Future works will include the development of functional prototypes to be installed in real vehicles and the validations of the concepts in real road conditions.

As a final general comment, the energy recovered in EHSAs has the clear advantage of being able to harvest energy that would otherwise be lost in the form of heat. The introduction of these systems in real vehicles must still overcome some technical difficulties, such as their reduction in weight and price. At the same time, a dynamic behavior similar to that of the shock absorbers they replace, including the comfort perceived by the passengers, must be ensured. Therefore, further research is necessary to make EHSA technically and economically viable.

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